

LECTURE 1

POPULAR SCIENCE AND ALGORITHMS.

AND HOW THEY ARE DIFFERENT FROM COMP 614/514.

(DISCLAIMER: WE WILL NOT COVER THEM IN DEPTH)

MULTI-AGENT LEARNING ALGORITHM: HOW A COMPUTER CAN PLAY STARCRAFT?

KEYWORDS: POLICY GRADIENT METHODS

E.G., : maximize θ $\hat{E}_t \left[\frac{\pi_\theta(a_t|s_t)}{\pi_{\theta_{old}}(a_t|s_t)} \cdot \hat{A}_t \right]$

π_θ IS STOCHASTIC POLICY
 \hat{A}_t : ESTIMATOR OF ADV. FUNCTION
 \hat{E}_t : EMPIRICAL AVERAGE

S.T. $\hat{E}_t \left[\text{KL}[\pi_{\theta_{old}}(\cdot|s_t), \pi_\theta(\cdot|s_t)] \right] \leq \delta$ TRPO

SOURCE: "PROXIMAL POLICY OPTIMIZATION ALGORITHMS"

OPENAI-FIVE: SCALED VERSION OF PROXIMAL POLICY OPTIMIZATION
 +
 LSTMS FOR EACH HERO
 =
 DEFEAT AMATEURS AT DOTA 2.

OF 180 YEARS OF PLAY WITHIN A DAY.

(VIDEO)

ALPHASTAR: BLIZZARD + DEEPMIND FOR STARCRAFT

ALSO CHECK: HOW TO PLAY TEXAS HOLD'EM, ...

(CONSTRAINED OPTIMIZATION) BEYOND SIMPLE SGD

GENERATING ADVERSARIAL LEARNING

KEYWORDS: IMAGE SYNTHESIS USING GANS.

SOURCE: "SEMANTIC IMAGE SYNTHESIS WITH STATISTICALLY-ADAPTIVE NORMALIZATION"

Gau Gau : SYNTHESIZE IMAGES FROM SEGMENTATION MAPS (VIDEO)

(MIN-MAX PROBLEMS)

NEURAL MACHINE TRANSLATION

KEYWORDS: CROSS-LINGUAL PRETRAINING, SELF-SUPERVISED LEARNING. BACK-TRANSLATION, TRANSFORMERS,

SOURCE: "FB FAIR'S NMT19 NEWS TRANSLATION TASK SUBMISSION"

(BEYOND SGD)

FAST COMBINATORIAL OPTIMIZATION ALGORITHMS

KEYWORDS : (INSPIRED BY) QUANTUM ADIABATIC OPTIMIZATION, BIFURCATION, ISING MODELS (= MAXCUT).

OVERVIEW OF COMP 414/514.

- GRADIENT DESCENT : CONVEX & NON-CONVEX.
- CONDITIONAL GRADIENT (FRANK WOLFE)
- NEWTON'S METHOD, QUASI-NEWTON TECHNIQUES
- MOMENTUM METHODS
- SGD & VARIANTS.
- SPARSITY-BASED METHODS
- LOW-RANK METHODS
- LANDSCAPE OF SMOOTH FUNCTIONS
- DISTRIBUTED IMPLEMENTATIONS

NON-CONVEX ALGORITHMS

COMMON THEME:
THEORY
+
PRACTICE.

OVERVIEW OF COMP 545.

- ALGORITHMS FOR MODERN SMOOTH UNCONSTRAINED OPTIMIZATION (ADAGRAD, RMSPROP, ADAM)
- CONSTRAINED OPTIMIZATION & DUALITY THEORY
- MIRROR DESCENT & MWU ALGORITHM.
- INTERIOR POINT METHODS (PRIMAL MOSTLY)
- FOCUS: ADVERSARIAL ROBUSTNESS AND STABILITY.
- SADDLE-POINT OPTIMIZATION, MIN-MAX, GANS.
- DISCRETE OPTIMIZATION TO CONVEXITY, AND BACK (SPECIAL TALK: MAXCUT AND HYPERSPHERICAL COORDINATES)
- QUANTUM COMPUTATION: INTRO, FAMOUS ALGORITHMS, HYBRID ALGO'S
- UNCERTAINTY IN ML: INFERENCE, GPs.

(BACKUP TOPICS: * - SUPERVISED LEARNING, DFO METHODS, SKETCHING + LINEAR ALGEBRA, LATEST NN ARCHITECTURES).

LOGISTICS.

- IN CONTRAST TO COMP 414/514: NO SLIDES, NO CODE - ONLY HANDWRITTEN NOTES
- FOR GRADUATE STUDENTS MOSTLY.

INTERLUDE

- GENERAL OPTIMIZATION

$$\min_{x \in \mathbb{R}^p} f(x) \quad \text{OR} \quad \min_{x \in \mathbb{R}^p} f(x)$$
$$\text{s.t. } g(x) \leq 0$$

PROVIDE SOME EXAMPLES:

1. LEAST SQUARES.
2. MATRIX REGRESSION
3. 2-HIDDEN LAYER MLP.

YOU SHOULD KNOW: VECTOR NOTATION + PROPERTIES

INNER PRODUCT

NORMS (l_2, l_1, l_∞, l_0)

MATRIX NOTATION

MATRIX MULTIPLICATION

INNER PRODUCT (MATRIX)

EIG/SVD

- GRADIENT DESCENT.

YOU SHOULD KNOW: DERIVATIVES & GRADIENT

HESSIAN AND ITS GEOMETRICAL INTERPRETATION

$$\nabla^2 f(\cdot) > 0, < 0, \geq 0 \dots$$

TAYLOR APPROXIMATION

LIPSCHITZ CONDITION

-||- GRADIENT CONDITION

$$\text{GD: } x_{t+1} = x_t - \eta_t \nabla f(x_t) \longrightarrow$$

WHAT CAN WE SAY ABOUT:

- i) η_t ?
- ii) INITIALIZATION?
- iii) CONVERGENCE?
- iv) ...

CONVERGENCE THM: CLAIM 6.

OVERVIEW OF CONV. RATES.



- CONVEXITY.

DEFINITION: $f(\alpha x + (1-\alpha)y) \leq \alpha f(x) + (1-\alpha)f(y)$, $\alpha \in [0,1]$

$$f(x) \geq f(y) + \langle \nabla f(y), x - y \rangle$$

GRADIENT DESCENT UNDER CONVEXITY: COMPARE WITH ABOVE

STRONG CONVEXITY AND GUARANTEES.

LOWER BOUNDS

CONVEX SETS & PROJECTIONS



- BEYOND FIRST-ORDER METHODS

- NEWTON'S METHOD. + GUARANTEES

- QUASI-NEWTON METHODS



- MOMENTUM ACCELERATION.

HEAVY BALL METHOD VS NESTEROV (SCHEMAS

GUARANTEES.



SGD.